# Mini Guide to Understanding the Bare <br> <br> Minimum about <br> <br> Minimum about Generative AI 

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## 1 Artificial Intelligence

Artificial Intelligence (AI) is not new, however, we are in a critical phase where we have (a) computers that are fast enough to fit large models, and (b) we have enough digital content to allow machines to "learn".

An important class of AI models rely on learning from pre-defined good answers: "supervised learning." For example: we show the AI pictures and tell it when there is a cat in it. The Al learns to recognise pictures with cats. Given enough pictures, it seems like the machine recognises cats just like us.

## 2 Linear Regressions

Linear regressions also "learn" from data. However, there is no lengthy learning process because we can calculate the coefficients.

To fit the linear model

$$
y=a x+b
$$

we seek $a$ and $b$ so that the differences between the observation $y_{i}$ and the estimate $\hat{y}_{i}$ are as small as possible: we minimise the sum of squares:

$$
\min _{a, b}\left(\sum_{i=1}^{N}\left(y_{i}-\hat{y}_{i}\right)^{2}\right)
$$

Solving this, we find the estimate for $a$ and $b$ to be as follows:

$$
\begin{aligned}
& \hat{a}=\frac{\sigma_{x, y}}{\sigma_{x}^{2}}=\rho_{x, y} \frac{\sigma_{y}}{\sigma_{x}}=\frac{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)\left(y_{i}-\hat{y}\right)}{\sum_{i=1}^{n}(x-\bar{x})^{2}} \\
& \hat{b}=\bar{y}-(\hat{a} \bar{x})
\end{aligned}
$$

For example, we want to predict fuel consumption as miles per gallon (mpg) for cars, based on their weight (wt), using the famous data set mtcars.

We can calculate the values of $a$ and $b$ for the linear regression.

$$
m p g=a w t+b
$$

The results can then be visualised as follows.


Figure 1: Fitting the model is finding the blue line that minimises (the square of) the distances between the red dots (observations) and blue dots (the estimates by the model).

## P Note: the machine learning

Note that we don't call a linear regression "Al" or "machine learning". This is because we can calculate the $a$ and $b$ (from the formula $\hat{y}=a x+b$ ). To call something "machine learning" we want a long learning process instead of a calculation.

### 2.1 Minorities

Models that are fitted so that total sum of deviations is minimal, do not necessarily work well for small sub-groups.

For example, in Figure 2 we show that small city cars see their fuel consumption on average overstated, and the fuel consumption is much more sensitive to the weight of a car (green) than the overall model (blue) would lead us to believe.


Figure 2: Small city cars (green) see their fuel consumption more over-stated than others. They are a minority and the model fails to capture their specific nature that is more sensitive to weight.

### 2.2 Multiple Linear Regression

To predict mpg, we can use more than one parameter. For example, we can use wt (weight), and hp (horsepower):

$$
m p g=a_{1} w t+a_{2} h p+b
$$

Also the parameters in this model can be calculated exactly and we do not consider this as AI.

## In the Big R-Book: Part V

Chapter 21 explains how linear regressions work and how to implement them in R.

## 3 Artificial Neural Networks

## Let's start with visualising our linear regression



Figure 3: This model estimates mpg as the weight (wt) multiplied with -3.87751 , then adds horsepower (hp) multiplied with -0.03178 and adds 37.22666 .

Well, you have imagined a most simple neural network with just one neuron. Now imagine a network of regressions feeding into each other as follows:


Figure 4: an Artificial Neural Network with 2 hidden layers of 2 neurons.

Each circle is called a "node". Apart from the input layer (leftmost) we can imagine in each circle a regression that uses the output of the previous layer as input. All parameters are chosen so that the sum of squares of differences between observations and model has to be as small as possible.

We cannot calculate the parameters anymore, and hence we need an iterative algorithm: the model needs to "learn" by trying variations and subsequently keeping the best variations.

Congratulations, you have imagined an Artificial Neural Network (ANN)!
Your ANN is simple: has 2 input nodes wt (weight)
and hp (horsepower). We can use more input nodes, more hidden layers, and more more neurons on those hidden layers.


Figure 5: An Artificial Neural Network with 3 hidden layers of respectively 4,3 , and 2 neurons.

This simple model has 61 variables . . . and it becomes impossible to understand why a high or low mpg is predicted.

## P Note: black box models

An ANN has so many parameters that it is impossible for us to understand the concept behind each node. Therefore we call it a "black box": it is not transparent and we cannot be sure why a given decision is made.

## In the Big R-Book: Part V

Artificial Neural Networks are described in my book in section V , chapter 23.

## 4 Large Language Models

Now imagine an ANN trained on all texts digitally available. Such model will have many internal layers and billions of parameters. The AI is trained to predict the next word (auto-regressive) or missing word (masked learning). Used in sequence this method creates sentences.

Allow the AI to learn on the data (unsupervised learning), and add some fine tuning (people providing the right answers and call this RHLF (reinforced learning from human feedback)).

Congratulations, you have imagined a large language model (LLM)!

### 4.1 The Transofrmer

It appears that one further step is needed: the "transformer".

The English Language, for example,has 147,000 words in use (and 47,000 words that are obsolete), but the economist uses only 35,000 different words, some sequences of words mean something else than the indidvidual words, some must be understood together (grandfather in my mother's side, etc.)

Hence we need to find one unique universal meaning of words: a virtual space with many thousands of dimensions. Eg. the word sequence
"brick house" could be:

$$
1034,55446,88,-8999, \ldots, 66676
$$

Eg., some words have a similar meaning: eg. a red house, a brick hourse, a house of bricks and mortar, a house with outsanding masonery, (in America a "lasting house" would mean the same too), etc.
Those words will get a similar encoding but differ eg. in the dimensions that refer to how formal or poetic the text is. For example "red house" could be

$$
10,554,101,-8756, \ldots, 66170
$$

## 5 Generative AI

You also heard the term "generative Al". Well, that is the wider term for Al that is able to be creative in the sense that it can create things that didn't exist before. Well-known examples are structural design elements, images, and text (the LLMs).

An Al that generates pictures will be constructed and trained differently than an AI that provides conversations, but the basic principles are the same.

## 6 Add Some Magic

If you believe now that Al does slavishly what it is taught to do, then read on.

### 6.1 Emergent Abilities

LLMs might acquire the ability to do something that they are not trained for. Given a critical level of complexity, they just can do it.

For example, LLMs seem to be able to speak Hinglish (combined English and Hindi), without being trained for it. Other emergent abilities are passing college-level exams, do multi-step arith-
metic, identify the intended meaning of a word out of the context, etc.

## - Note: Emergent Abilities

Already now, in the infancy of AI, we have models that display "emergent abilities": they can do things that they weren't really taught to do.

### 6.2 Hallucinations

Sometimes the LLM will confidentially assert something that does not follow from the data.
For example without fine tuning, most LLMs will
answer "no" to the question "Can I teach an old dog new tricks." This is because of the popular expression "One cannot teach an old dog new tricks?"

## P Note: hallucinations

LLMs can "hallucinate": they can make mistakes or show bias even when the data does not really have that mistake or bias. Those mistakes appear without warning!

## 7 Conclusions

- Al is in its infancy, and already now the results are amazing. It is the future and will be transformative.
- The abilities of large language models and generative Al are based on association, just as in a linear regression. There is no magic, nor conceptual understanding. They pretend, and they are good at it.
- Just as a linear regression, the LLM might miss-understand smaller groups. However, the problem of over-fitting is almost to be expected (assuming that specific patterns
from the data apply to the wider groups)
- LLMs can gain abilities that we didn't directly teach them and they can hallucinate.
- Use such models (it is the future), but always remain in the driving seat! Don't let your guard down.
- The rise of Al creates massive ethical and societal issues: more about that in next editions.


## 8 Background

This was one small piece of data science. The "Big R-Book: From Data Science to Learning Machines and Big Data" helps you to to get started with data science.

The homepage of the books is:
www.de-brouwer.com/r-book

THE
BIG R-BOOK
FROM DATA SCIENCE TO LEARNING
MACHINES AND BIG DATA


## 9 Nomenclature

## Nomenclature

$\bar{x}$ the bar above a variable refers to the mean of the variable
$\hat{a}$ the estimate for the coefficient a
$\rho_{x, y}$ correlation between the variable $x$ and $y$
$\sigma_{x, y}$ covariance between the variable $x$ and $y$
$\sigma_{x}$ variance of the variable $x$
$a$ the coefficient in the linear regression $y=$ $a x+b$
$x \quad x$ is a variable (column name) that we use to explain $y$
$x_{i}$ the index $i$ refers to the number of the row (observation $i$ )
$y \quad y$ is the variable (column name) that we want to predict using $x$

AI Artificial Intelligence
ANN artificial neural network
LLM large language model
RHLF reinforced learning from human feedback

